

Algebra 2 CC

Name \_\_\_\_\_ ID: 1

## Radical Practice Worksheet

Date \_\_\_\_\_ Period \_\_\_\_\_

**Solve each equation. Remember to check for extraneous solutions.**

1)  $\sqrt{4n} = \sqrt{6 - 2n}$

2)  $\sqrt{15 - 2x} = \sqrt{10 - x}$

3)  $\sqrt{3x - 23} = 2$

4)  $14 = \sqrt{\frac{a}{3}} + 9$

5)  $\sqrt{2a - 6} = a - 3$

6)  $\sqrt{3p - 20} = p - 6$

7)  $b - 5 = \sqrt{6b - 35}$

8)  $4 + \sqrt{15r + 1} = 8$

9)  $-4 = \sqrt{\frac{m}{2}} - 5$

10)  $\sqrt{-5 - 3a} - \sqrt{-3 - a} = 2$

11)  $\sqrt{-5 - 6r} - \sqrt{-6 - 2r} = 3$

12)  $\sqrt{2k + 10} = 3 - \sqrt{-2 - 9k}$

**Simplify.**

13)  $5\sqrt{15}(\sqrt{10} + 2\sqrt{6})$

14)  $-4\sqrt{3}(4\sqrt{5} + \sqrt{6})$

**Write each expression in exponential form.**

15)  $(\sqrt{r})^3$

16)  $(\sqrt{5m})^3$

17)  $(\sqrt{3n})^3$

18)  $(\sqrt[4]{3x})^3$

19)  $(\sqrt[4]{3n})^5$

20)  $(\sqrt[6]{2b})^7$

**Simplify.**

21)  $\sqrt[3]{-54b^8}$

22)  $\sqrt[3]{375b^4}$

23)  $\sqrt{18m^3}$

24)  $\sqrt{294r^2}$

25)  $\sqrt{245n^3}$

26)  $\sqrt{128b^4}$

27)  $\frac{4\sqrt{5}}{4\sqrt{125}}$

28)  $\frac{4\sqrt{20}}{2\sqrt{5}}$

29)  $\frac{4\sqrt{4}}{\sqrt{100}} = \frac{4 \cdot 2}{10} = \frac{8}{10} = \frac{4}{5}$

30)  $\frac{5\sqrt{3}}{\sqrt{4}}$

31)  $\frac{4\sqrt{15}}{4\sqrt{3}}$

32)  $\frac{4\sqrt{6}}{\sqrt{3}}$

33)  $2\sqrt{2} + 2\sqrt{5} + 3\sqrt{2}$

34)  $-3\sqrt{8} - \sqrt{20} + 3\sqrt{45}$

35)  $2\sqrt{3} - 2\sqrt{3} + 3\sqrt{12}$

36)  $-\sqrt{24} + 3\sqrt{54} - \sqrt{12}$

$$1) (\sqrt{4n})^2 = (\sqrt{6-2n})^2$$

$$\begin{array}{r} 4n = 6 - 2n \\ +2n \quad +2n \\ \hline \end{array}$$

$$\frac{6n}{6} = \frac{6}{6}$$

$$n = 1$$

$$2) (\sqrt{15-2x})^2 = (\sqrt{10-x})^2$$

$$15 - 2x = 10 - x$$
$$\begin{array}{r} +2x \qquad +2x \\ \hline \end{array}$$

$$15 = 10 + x$$

$$5 = x$$

$$3) (\sqrt{3x-23} = 2)^2$$

$$3x - 23 = 4$$

$$3x = 27$$

$$x = 9$$

$$4) 14 = \sqrt{\frac{a}{3}} + 9$$

$$\frac{-9}{-9} \quad \frac{-9}{-9}$$

$$(5)^2 = \left(\sqrt{\frac{a}{3}}\right)^2$$

$$(3)25 = \frac{a}{3} (3)$$

$$75 = a$$

~~$$(14)^2 = \left(\sqrt{\frac{a}{3}} + 9\right)^2$$

$$196 = \left(\sqrt{\frac{a}{3}} + 9\right)\left(\sqrt{\frac{a}{3}} + 9\right)$$

$$196 = \frac{a}{3} + 18\sqrt{\frac{a}{3}} + 81$$~~

$$5) (\sqrt{2a-6})^2 = (a-3)^2$$

$$2a-6 = (a-3)^2$$

$$2a-6 = (a-3)(a-3)$$

$$2a-6 = a^2 - 3a - 3a + 9$$

$$2a-6 = a^2 - 6a + 9$$

$$\begin{array}{r} -2a \\ \hline \end{array}$$

$$\begin{array}{r} -6 = a^2 - 6a + 9 \\ +6 \qquad \qquad \qquad +6 \\ \hline \end{array}$$

$$0 = a^2 - 6a + 15$$

$$\begin{array}{l} \swarrow \quad \searrow \\ 3 \cdot 5 = +8 \\ -3 \cdot -5 = -8 \end{array}$$

$$0 = (a-3)(a-5)$$

$$a-3=0 \quad a-5=0$$

$$a=3$$

$$a=5$$

$$10) (\sqrt{-5-3a} - \sqrt{-3-a})^2$$

$$(\sqrt{-5-3a} - \sqrt{-3-a})(\sqrt{-5-3a} - \sqrt{-3-a})$$

$$(\sqrt{-5-3a})(\sqrt{-5-3a})$$

$$-5-3a$$

$$+ (\sqrt{-3-a})(\sqrt{-3-a})$$

$$-3-a$$



$$10) \sqrt{-5-3a} - \sqrt{-3-a} = 2$$

$$(\sqrt{-5-3a} - \sqrt{-3-a})(\sqrt{-5-3a} + \sqrt{-3-a})$$

$$10) \sqrt{-5-3a} - \sqrt{-3-a} = 2$$

$$\{-3, -7\}$$

$$10) \sqrt{-5-3a} - \sqrt{-3-a} = 2$$

$$(\sqrt{-5-3a} - \sqrt{-3-a})(\sqrt{-5-3a} + \sqrt{-3-a})$$

$$-5-3a \quad \sqrt{-5-3a} \cdot \sqrt{-3-a} \quad -3a-a$$

$$\sqrt{-3-a} \cdot \sqrt{-5-3a}$$

$$2\sqrt{-5-3-3a-3a}$$

$$a \cdot 3 \cdot 2\sqrt{15} \cdot 9$$

$$-5-3a + 6a\sqrt{15} - 3a - a$$

$$1) (\sqrt{4n}) = (\sqrt{6-2n})$$

$$(\sqrt{4n})^2 = (\sqrt{6-2n})^2$$

$$\begin{array}{r} 4n = 6 - 2n \\ + 2n \quad + 2n \\ \hline \end{array}$$

$$\frac{6n}{6} = \frac{6}{6}$$

$$n = 1$$

$$2) (\sqrt{15-2x})^2 = (\sqrt{10-x})^2$$

$$\begin{array}{r} 15-2x = 10-x \\ -10 \quad -10 \\ \hline \end{array}$$

$$\begin{array}{r} 5-2x = -x \\ +2x \quad +2x \\ \hline 5 = x \end{array}$$

$$3) (\sqrt{3x-23})^2 = (2)^2$$

$$3x - 23 = 4$$

$$3x = 27$$

$$x = 9$$

$$4) 14 = \sqrt{\frac{a}{3} + 9}$$

$$\begin{array}{r} -9 \\ -9 \end{array}$$

$$(5)^2 = \left(\sqrt{\frac{19}{3}}\right)^2$$

$$(3) 25 = \frac{a}{3} \quad (3)$$

$$75 = a$$

Time out !!

$$(14)^2 = \left(\sqrt{\frac{a}{3} + 9}\right)^2$$

$$196 = \left(\sqrt{\frac{a}{3} + 9}\right)\left(\sqrt{\frac{a}{3} + 9}\right)$$

$$\frac{a}{3} + 9\sqrt{\frac{a}{3}} \quad 9\sqrt{\frac{a}{3}} + 81$$

$$5) (\sqrt{2a-6})^2 = (a-3)^2$$

$$2a-6 = (a-3)(a-3)$$

$$2a-6 = a^2 - 6a + 9$$

$$\begin{array}{r} +6 \\ \hline \end{array}$$

$$2a = a^2 - 6a + 15$$

$$\begin{array}{r} -2a \\ \hline \end{array}$$

$$0 = a^2 - 8a + 15$$

$$0 = (a-5)(a-3)$$

1 · 15	-1 · -15
5 · 3	-5 · -3

a=5
a=3

GCF  
FACTOR

$$\frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$1) \frac{\sqrt{4n}}{\sqrt{4n}} = \frac{\sqrt{6-2n}}{\sqrt{4n}}$$

$$\sqrt{4n} \quad \sqrt{4n}$$

$$1 = \frac{\sqrt{6-2n}}{\sqrt{4n}}$$



17)  $(\sqrt{3n})^3$

18)  $(\sqrt[4]{3x})^3$

19)  $(\sqrt[4]{3n})^5$

~~$(\sqrt{\quad})^2$~~

20)  $(\sqrt[6]{2b})^7$

19)

$$(\sqrt[4]{3n})(\sqrt[4]{3n})(\sqrt[4]{3n})(\sqrt[4]{3n})(\sqrt[4]{3n})$$

~~$(\sqrt[4]{3n})^4$~~

$$3n(\sqrt[4]{3n})$$

18)  $(\sqrt[4]{3x})^3$

$$(\sqrt[4]{3x})(\sqrt[4]{3x})(\sqrt[4]{3x})$$

$$(\sqrt[4]{3x})^3 \text{ answer}$$

20)  $(\sqrt[6]{2b})^7$

$$(\sqrt[6]{2b})(\sqrt[6]{2b})(\sqrt[6]{2b})(\sqrt[6]{2b})(\sqrt[6]{2b})(\sqrt[6]{2b})(\sqrt[6]{2b})(\sqrt[6]{2b})$$

$$\begin{array}{c} \downarrow \\ \left( \frac{2b}{\sqrt[6]{2b}} \right) \left( \sqrt[6]{2b} \right) \\ \downarrow \\ 2b \left( \sqrt[6]{2b} \right) \end{array}$$

21)  $\sqrt[3]{+54b^8}$

$\sqrt[3]{+54} \cdot \sqrt[3]{b^8}$

$\sqrt[3]{27 \cdot 2} \cdot \sqrt[3]{b \cdot b \cdot b \cdot b \cdot b \cdot b \cdot b \cdot b}$

$\sqrt[3]{27} \cdot \sqrt[3]{2} \cdot b \cdot b \cdot \sqrt[3]{b^2}$

$3\sqrt[3]{2} \cdot b \cdot b \cdot \sqrt[3]{b^2}$

$3b^2 \sqrt[3]{2b^2}$

answer

1	$1^3 = 1$	$\sqrt[3]{1} = 1$
2	$2^3 = 8$	$\sqrt[3]{8} = 2$
3	$3^3 = 27$	$\sqrt[3]{27} = 3$
4	$4^3 = 64$	$\sqrt[3]{64} = 4$
5	$5^3 = 125$	$\sqrt[3]{125} = 5$
6	$6^3 = 216$	$\sqrt[3]{216} = 6$
7	$7^3 = 343$	$\sqrt[3]{343} = 7$

17)  $(\sqrt{3n})^3$

18)  $(\sqrt[4]{3x})^3$  answer  
( ) ( ) ( )

19)  $(\sqrt[4]{3n})^5$

20)  $(\sqrt[6]{2b})^7$

17)  $(\sqrt{3n})^3$

$(\sqrt[2]{3n})(\sqrt[2]{3n})(\sqrt[2]{3n})$

$(\sqrt[2]{3n})^2$

$3n\sqrt{3n}$  answer

19)  $(\sqrt[4]{3n})^5$

$(\sqrt[4]{3n})(\sqrt[4]{3n})(\sqrt[4]{3n})(\sqrt[4]{3n})(\sqrt[4]{3n})$

$(\sqrt[4]{3n})^4$   $(\sqrt[4]{3n})$

$3n(\sqrt[4]{3n})$

answer

$$20) (\sqrt[6]{2b})^7$$

$$(\sqrt[6]{2b})(\sqrt[6]{2b})(\sqrt[6]{2b})(\sqrt[6]{2b})(\sqrt[6]{2b})(\sqrt[6]{2b})(\sqrt[6]{2b})$$

$$\cancel{(\sqrt[6]{2b})}$$

$$= 2b(\sqrt[6]{2b})$$

$$1) (\sqrt{4n})^2 = (\sqrt{6-2n})^2$$

$$4n = 6 - 2n$$
$$\begin{array}{r} + 2n \quad + 2n \\ \hline \end{array}$$

$$\frac{6n}{6} = \frac{6}{6}$$

$$n = 1$$

$$2) (\sqrt{15-2x})^2 = (\sqrt{10-x})^2$$

$$15-2x = 10-x$$

$$\begin{array}{r} +2x \quad +2x \\ \hline \end{array}$$

$$15 = 10 + x$$

$$\begin{array}{r} -10 \quad -10 \\ \hline \end{array}$$

$$5 = x$$



$$3) (\sqrt{3x-23})^2 = 2^2$$

$$3x - 23 = 4$$
$$\begin{array}{r} +23 \quad +23 \\ \hline \end{array}$$

$$3x = 27$$
$$\begin{array}{r} \overline{3} \quad \overline{3} \end{array}$$

$$x = 9$$

$$4) 14 = \sqrt{\frac{a}{3}} + 9$$

$$\begin{array}{r} -9 \\ \hline (5)^2 = \left(\sqrt{\frac{a}{3}}\right)^2 \end{array}$$

$$(3) 25 = \left(\frac{a}{3}\right) 3$$

$$75 = a$$

What if...

$$(14)^2 = \left(\sqrt{\frac{a}{3}} + 9\right)^2$$

$$\left(\sqrt{\frac{a}{3}} + 9\right)\left(\sqrt{\frac{a}{3}} + 9\right)$$

$$5) (\sqrt{2a-6})^2 = (a-3)^2$$

$$2a-6 = (a-3)^2$$

$$2a-6 = (a-3)(a-3)$$

$$2a-6 = a^2 - 6a + 9$$

$$-6 = a^2 - 8a + 9$$

$$0 = a^2 - 8a + 15$$

$$0 = (a-3)(a-5)$$

$\begin{array}{l} 1 \cdot 15 \\ 3 \cdot 5 \\ -1 \cdot -15 \\ -3 \cdot -5 \end{array}$

$a=3$     $a=5$

① FACTOR

② GCF

③  $\frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$

$$6) \sqrt{3p - 20} = p - 6$$

$$17) (\sqrt[4]{3n})^3 \quad (\sqrt{3n})^2 (\sqrt{3n})$$

$$\quad \downarrow \quad \quad \downarrow$$

$$\quad 3n \quad \sqrt{3n}$$

18)  $(\sqrt[4]{3x})^3$

19)  $(\sqrt[4]{3n})^5$

20)  $(\sqrt[6]{2b})^7$

**Simplify.**

21)  $\sqrt[3]{-54b^8}$

22)  $\sqrt[3]{375b^4}$

23)  $\sqrt{18m^3}$

24)  $\sqrt{294r^2}$

25)  $\sqrt{245n^3}$

26)  $\sqrt{128b^4}$

27)  $\frac{4\sqrt{5}}{4\sqrt{125}}$

28)  $\frac{4\sqrt{20}}{2\sqrt{5}}$

29)  $\frac{4\sqrt{4}}{\sqrt{100}}$

30)  $\frac{5\sqrt{3}}{\sqrt{4}}$

31)  $\frac{4\sqrt{15}}{4\sqrt{3}}$

32)  $\frac{4\sqrt{6}}{\sqrt{3}}$

33)  $2\sqrt{2} + 2\sqrt{5} + 3\sqrt{2}$

34)  $-3\sqrt{8} - \sqrt{20} + 3\sqrt{45}$

35)  $2\sqrt{3} - 2\sqrt{3} + 3\sqrt{12}$

36)  $-\sqrt{24} + 3\sqrt{54} - \sqrt{12}$

**Simplify.**

21)  $\sqrt[3]{-54b^8}$

$$\sqrt[3]{54b^8}$$

$$\sqrt[3]{\boxed{3 \cdot 3 \cdot 3} \cdot 2 \cdot \underbrace{b \cdot b \cdot b \cdot b \cdot b \cdot b}_6}$$

$$\sqrt[3]{(3)^3 \cdot 2 \cdot b^2 \cdot \sqrt[3]{b^2}}$$

$$\frac{54}{27} = 2$$

$$3 \cdot 3 \cdot 3 = 27$$

$$(3)^3 = 27$$

$$3i\sqrt{2} \quad b^2\sqrt[3]{b^2}$$

$$\boxed{3b^2i\sqrt[3]{2b^2}}$$

17)  $(\sqrt[4]{3n})^3 = 3n \sqrt{3n}$

18)  $(\sqrt[4]{3x})^3$

19)  $(\sqrt[4]{3n})^5$

20)  $(\sqrt[6]{2b})^7$

$2b^6 \sqrt[6]{2b}$

$(\sqrt[4]{3n})^5$

~~$(\sqrt[7]{3n})^2 = 3n$~~

$(\sqrt[4]{3n})^4 (\sqrt[4]{3n})^1$

~~$(\sqrt[3]{3n})^3 = 3n$~~

~~$(\sqrt[4]{3n})^4 = 3n$~~

$(\sqrt[4]{3n})(\sqrt[4]{3n})(\sqrt[4]{3n})(\sqrt[4]{3n})(\sqrt[4]{3n})$

~~$(\sqrt[4]{3n})^4$~~   $(\sqrt[4]{3n})$

$3n \sqrt[4]{3n}$  answer

Algebra 2 CC

Name \_\_\_\_\_ ID: 1

## Radical Practice Worksheet

Date \_\_\_\_\_ Period \_\_\_\_\_

**Solve each equation. Remember to check for extraneous solutions.**

$$1) \sqrt{4n} = \sqrt{6-2n}$$

$$\{1\}$$

$$2) \sqrt{15-2x} = \sqrt{10-x}$$

$$\{5\}$$

$$3) \sqrt{3x-23} = 2$$

$$\{9\}$$

$$4) 14 = \sqrt{\frac{a}{3}} + 9$$

$$\{75\}$$

$$5) \sqrt{2a-6} = a-3$$

$$\{3, 5\}$$

$$6) \sqrt{3p-20} = p-6$$

$$\{7, 8\}$$

$$7) b-5 = \sqrt{6b-35}$$

$$\{6, 10\}$$

$$8) 4 + \sqrt{15r+1} = 8$$

$$\{1\}$$

$$9) -4 = \sqrt{\frac{m}{2}} - 5$$

$$\{2\}$$

$$10) \sqrt{-5-3a} - \sqrt{-3-a} = 2$$

$$\{-3, -7\}$$

$$11) \sqrt{-5-6r} - \sqrt{-6-2r} = 3$$

$$\left\{-\frac{7}{2}, -5\right\}$$

$$12) \sqrt{2k+10} = 3 - \sqrt{-2-9k}$$

$$\text{No solution.}$$

**Simplify.**

$$13) 5\sqrt{15}(\sqrt{10} + 2\sqrt{6})$$

$$25\sqrt{6} + 30\sqrt{10}$$

$$14) -4\sqrt{3}(4\sqrt{5} + \sqrt{6})$$

$$-16\sqrt{15} - 12\sqrt{2}$$

**Write each expression in exponential form.**

$$15) (\sqrt{r})^3$$

$$r^{\frac{3}{2}}$$

$$16) (\sqrt{5m})^3$$

$$(5m)^{\frac{3}{2}}$$



$$17) (\sqrt{3n})^3$$

$$(3n)^{\frac{3}{2}}$$

$$19) (\sqrt[4]{3n})^5$$

$$(3n)^{\frac{5}{4}}$$

Simplify.

$$21) \sqrt[3]{-54b^8}$$

$$-3b^2\sqrt[3]{2b^2}$$

$$23) \sqrt{18m^3}$$

$$3m\sqrt{2m}$$

$$25) \sqrt{245n^3}$$

$$7n\sqrt{5n}$$

$$27) \frac{4\sqrt{5}}{4\sqrt{125}}$$

$$\frac{1}{5}$$

$$29) \frac{4\sqrt{4}}{\sqrt{100}}$$

$$\frac{4}{5}$$

$$31) \frac{4\sqrt{15}}{4\sqrt{3}}$$

$$\sqrt{5}$$

$$33) 2\sqrt{2} + 2\sqrt{5} + 3\sqrt{2}$$

$$5\sqrt{2} + 2\sqrt{5}$$

$$35) 2\sqrt{3} - 2\sqrt{3} + 3\sqrt{12}$$

$$6\sqrt{3}$$

$$18) (\sqrt[4]{3x})^3$$

$$(3x)^{\frac{3}{4}}$$

$$20) (\sqrt[6]{2b})^7$$

$$(2b)^{\frac{7}{6}}$$

$$22) \sqrt[3]{375b^4}$$

$$5b\sqrt[3]{3b}$$

$$24) \sqrt{294r^2}$$

$$7r\sqrt{6}$$

$$26) \sqrt{128b^4}$$

$$8b^2\sqrt{2}$$

$$28) \frac{4\sqrt{20}}{2\sqrt{5}}$$

$$4$$

$$30) \frac{5\sqrt{3}}{\sqrt{4}}$$

$$\frac{5\sqrt{3}}{2}$$

$$32) \frac{4\sqrt{6}}{\sqrt{3}}$$

$$4\sqrt{2}$$

$$34) -3\sqrt{8} - \sqrt{20} + 3\sqrt{45}$$

$$-6\sqrt{2} + 7\sqrt{5}$$

$$36) -\sqrt{24} + 3\sqrt{54} - \sqrt{12}$$

$$7\sqrt{6} - 2\sqrt{3}$$