

Finding the mean  
Average

Population

$$\mu = \frac{\sum x}{N}$$

↑  
mu

↑  
sigma

↑  
# of data terms

Sample

$$\bar{X} = \frac{\sum x}{n}$$

↑  
"X bar"

↑  
sigma

↑  
# of data terms

A **measure of central tendency** is a value that represents a typical, or central, entry of a data set. The three most commonly used measures of central tendency are the mean, the median, and the mode.

### DEFINITION

The **mean** of a data set is the sum of the data entries divided by the number of entries. To find the mean of a data set, use one of the following formulas.

$$\text{Population Mean: } \mu = \frac{\sum x}{N} \quad \text{Sample Mean: } \bar{x} = \frac{\sum x}{n}$$

The lowercase Greek letter  $\mu$  (pronounced mu) represents the population mean and  $\bar{x}$  (read as "x bar") represents the sample mean. Note that  $N$  represents the number of entries in a *population* and  $n$  represents the number of entries in a *sample*. Recall that the uppercase Greek letter sigma ( $\Sigma$ ) indicates a summation of values.

Find the mean.

$$\begin{aligned} & \textcircled{50}, \underline{\underline{75}}, \underline{\underline{88}}, \textcircled{92}, \underline{\underline{78}} = 76.6 \\ & \boxed{88}, \boxed{93}, \underline{\underline{79}}, \textcircled{85}, \textcircled{90} = 87 \\ & \textcircled{50}, \underline{\underline{65}}, \textcircled{60}, \textcircled{90}, \textcircled{95} = 72 \end{aligned}$$

## Population

mean  
"average"

$$\mu = \frac{\sum x}{N}$$

↑  
mu

← sigma

## Sample

mean  
"average"

$$\bar{x} = \frac{\sum x}{n}$$

↑  
"x bar"

← sigma

Population Mean:  $\mu = \frac{\sum x}{N}$

Sample Mean:  $\bar{x} = \frac{\sum x}{n}$

$\mu =$

$\bar{x}$

$N =$  population  
# in the  
population

$n =$  sample  
# in sample

Mean : Avg.  $n$  and  $\bar{x}$

median : middle, put in numerical order

mode : # that occurs the most often

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median : 3, 5, 2, 8, 1, 6

~~1~~, ~~2~~, ~~3~~, ~~5~~, ~~6~~, ~~8~~

~~1~~, ~~2~~, 3, 5, ~~6~~, ~~8~~

$$\frac{3+5}{2} = \frac{8}{2} = 4$$

Test	40%
Quiz	30%
Hwk	5%
Midterm	5%
FR	5%
MC	15%

Test	40%	60, 45, 80, 85, 90
Quiz	30%	40, 50, 100, 88, 100
Hwk	5%	0, 0, 100, 100
midterm	5%	75
FR	5%	60
MC	15%	70



Test	40%	60, 45, 80, 85, 90	$\frac{60+45+80+85+90}{5} \cdot 40\%$
Quiz	30%	40, 50, 100, 88, 100	$\frac{40+50+100+88+100}{5} \cdot 30\%$
Hwk	5%	0, 0, 100, 100	$\frac{0+0+100+100}{4} \cdot 5\%$
Midterm	5%	75	$75 \cdot 5\%$
FR	5%	60	$60 \cdot 5\%$
MC	15%	70	$70 \cdot 15\%$
		100%	
		100 pts.	

Test	40%	60, 45, 80, 85, 90	$\frac{60+45+80+85+90}{5} \cdot 40\%$	28.8
Quiz	30%	40, 50, 100, 88, 100	$\frac{40+50+100+88+100}{5} \cdot 30\%$	22.68
Hwk	5%	0, 0, 100, 100	$\frac{0+0+100+100}{4} \cdot 5\% \cdot 0.05$	2.5
Midterm	5%	75	$75 \cdot 5\%$	3.75
FR	5%	60	$60 \cdot 5\%$	3
mc	15%	70	$70 \cdot 15\%$	10.5
		100% 100 pts.		<hr/>
		100, 100, 100, 100	$100(.05) = 5$	71.23

$$\begin{array}{r}
 71.23 \\
 + 2.5 \\
 \hline
 73.73 \\
 \textcircled{\approx 74}
 \end{array}$$

midterm	40%	(70)	28	40
Final exam	60%			60
			42	

**DEFINITION**

A **weighted mean** is the mean of a data set whose entries have varying weights. A weighted mean is given by

$$\bar{x} = \frac{\sum(x \cdot w)}{\sum w}$$

where  $w$  is the weight of each entry  $x$ .

Test	40%	65, 78, 88	$\frac{(65+78+88)}{3} \cdot 40\% = 30.8$
Quiz	30%	50, 70, 90, 85	$(73.75) \cdot 30\% = 22.125$
Hwk	5%	0, 100, 100, 100	$(75) \cdot .05 = 3.75$
Midterm	5%	75	$= 3.75$
FR	5%	88	$= 4.4$
MC	15%	80	$= 12.0$
			$= 76.825$
			$\approx 77$

Handwritten notes: "points" with an arrow pointing to the Test row; "change to 5" with an arrow pointing to the MC weight; "100...?" with a circle around the 100 in the Hwk row; "A" with a circle around the 80 in the MC row.

Test	40%
Quiz	30%
Hwk	5%
Midterm	5%
FR	5%
MC	15%

Test 90, 88, 75, 80  
 Quiz 95, 80, 60, 100  
 Hwk 100, 100, 100, 100  
 Midterm 60

FR 65%  
 MC 70%