

# 6.1 Notes – Confidence Intervals for the Mean Part 2

(Large Sample)

## I. Estimating Population Parameters

**Part A.** A point estimate is a \_\_\_\_\_ for a \_\_\_\_\_.

Try It Yourself 1 pg 310

Market researchers use the number of sentences per advertisement as a measure of readability for magazine advertisements. The following represents a random sample of the number of sentences found in 30 magazine advertisements.

16 9 14 11 17 12 99 18 13 12 5 9 17 6 11  
17 18 20 6 14 7 11 12 12 5 11 18 6 4 13

Find a point estimate for the mean sentence length of the population.

**Part B.** An interval estimate is an \_\_\_\_\_.

To form an interval estimate, use the \_\_\_\_\_ as the \_\_\_\_\_, then add and subtract a \_\_\_\_\_.

Before finding an interval estimate, you should first determine \_\_\_\_\_ that your interval estimate contains the \_\_\_\_\_.

**Part C.** The level of confidence, \_\_\_\_\_, is the \_\_\_\_\_.

The level of confidence,  $c$ , is the area under the standard normal curve between the \_\_\_\_\_,

For instance, if  $c = 90\%$ , then how much area lies outside of the confidence interval?

How much would have to be in each tail?

What would the critical  $z$ -values be?

You try: If  $c = 96\%$ , what are the critical values? Sketch and label a picture.

The margin of error, \_\_\_\_\_, is the \_\_\_\_\_.

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When  $n \geq 30$ , the \_\_\_\_\_, \_\_\_\_\_, can be used in place of  $\sigma$ .

## Try It Yourself 2

Use the data given for Try It Yourself 1 and a 95% confidence interval to find the maximum error of estimate for the mean number of sentences in a magazine advertisement.

$n =$  \_\_\_\_\_       $s =$  \_\_\_\_\_ (use your calculator to find)       $z_c =$  \_\_\_\_\_

$E =$  \_\_\_\_\_

## II. Confidence Intervals for the Population Mean

Part A. A \_\_\_\_\_ for a population mean  $\mu$  is



The probability that the \_\_\_\_\_ contains  $\mu$  is \_\_\_\_\_.

### Guidelines:

Finding a Confidence Interval for a Population Mean ( $n \geq 30$  or  $\sigma$  known)

In words

In symbols

1.

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2.

3.

4.

5.

6. You MUST write your answer in the context of the problem.

“We are (enter confidence)% confident that the true mean (enter context of problem) is between (enter left endpoint) and (enter right endpoint).”

### Try It Yourself 3

Construct a 90% confidence interval for the mean number of sentences in a magazine

advertisement from Try It Yourself 1. Show your work.

**Conclusion:** We are \_\_\_\_\_ confident that the true mean \_\_\_\_\_ is between \_\_\_\_\_ and \_\_\_\_\_.

### Try It Yourself 4

Construct a 99% confidence interval for the mean number of sentences in a magazine advertisement from Try It Yourself 1. Show your work.

**Conclusion:**

*Analysis:* How do the intervals from Try It Yourself 3 and Try It Yourself 4 compare?

### Try It Yourself 5

A college admissions director wishes to estimate the mean age of all students currently enrolled. In a random sample of 20 students, the mean age is found to be 22.9 years.

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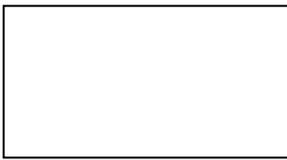
From past studies, the standard deviation is known to be 1.5 years. Construct a 95% confidence interval of the population mean age?

## Sample Size

As the level of confidence \_\_\_\_\_, the confidence interval \_\_\_\_\_. As the confidence interval \_\_\_\_\_, the precision of the estimate \_\_\_\_\_.

One way to improve the precision of an estimate without decreasing the level of confidence is to \_\_\_\_\_.

We can work backwards from the formula for the margin of error (maximum error of estimate) E.



If  $\sigma$  is \_\_\_\_\_, you can estimate it \_\_\_\_\_, provided you have a sample with \_\_\_\_\_.

## Try It Yourself 6

A college admissions director wishes to estimate the mean age of all students currently enrolled. From past studies, the standard deviation is known to be 5.5 years. How many students must be included in the sample if you want to be 95% confident that the sample mean is within two years of the population mean?

## Try It Yourself 7

You work for a consumer advocate agency and want to find the mean repair cost of a washing machine. From past studies, the standard deviation is known to be \$17.50. How many repairs must be included in the sample if you want to be 99% confident that the sample mean is within \$5.00 of the population mean?

Assignment: pg 320/ 56 – 58