

Vocabulary: Unit 2: Polynomial Functions

- **Coefficient:**
- **Degree:**
- **End Behavior:**
- **Fundamental Theorem of Algebra:**
- **Geometric Sequence:**
- **Geometric Series:**
- **Multiplicity: Pascal's Triangle:**
- **Polynomial:**
- **Rational Root Theorem:**
- **Relative Minimum:**
- **Relative Maximum:**
- **Remainder Theorem:**
- **Roots:**
- **Sum of a finite geometric series:**
- **Sum of an infinite geometric series:**
- **convergent**
- **divergent**
- **Synthetic Division:**
- **Zero:**

Vocabulary: Unit 2: Polynomial Functions

- **Coefficient:** a number multiplied by a variable.
- **Degree:** the greatest exponent of its variable
- **End Behavior:** the value of $f(x)$ as x approaches positive and negative infinity
- **Fundamental Theorem of Algebra:** every non-zero single-variable polynomial with complex coefficients has exactly as many complex roots as its degree, if each root is counted up to its multiplicity.
- **Geometric Sequence:** is a sequence with a constant ratio between successive terms
- **Geometric Series:** the expression formed by adding the terms of a geometric sequence
- **Multiplicity:** the number of times a root occurs at a given point of a polynomial equation.
- **Pascal's Triangle:** an arrangement of the values of ${}_nC_r$ in a triangular pattern where each row corresponds to a value of n
- **Polynomial:** a mathematical expression involving a sum of nonnegative integer powers in one or more variables multiplied by coefficients. A polynomial in one variable with constant coefficients can be written in $ax^2 + b$ form. $a_n x^n + a_{n-1} x^{n-1} + \dots + a_2 x^2 + a_1 x + a_0$
- **Rational Root Theorem:** a theorem that provides a complete list of all possible rational roots of a polynomial equation. It states that every rational zero of the polynomial equation $f(x) = a_n x^n + a_{n-1} x^{n-1} + \dots + a_2 x^2 + a_1 x + a_0$, where all coefficients are integers, has the following form: $\frac{p}{q} = \frac{\text{factors of constant term } a_0}{\text{factors of leading coefficient } a_n}$
- **Relative Minimum:** a point on the graph where the function is increasing as you move away from the point in the positive and negative direction along the horizontal axis.
- **Relative Maximum:** a point on the graph where the function is decreasing as you move away from the point in the positive and negative direction along the horizontal axis.
- **Remainder Theorem:** states that the remainder of a polynomial $f(x)$ divided by a linear divisor $(x - c)$ is equal to $f(c)$.
- **Roots:** solutions to polynomial equations.
- **Sum of a finite geometric series:** The sum, S_n , of the first n terms of a geometric sequence is given by $S_n = \frac{a_1 - a_1 r^n}{1 - r} = \frac{a_1(1 - r^n)}{1 - r}$ where a_1 is the first term and r is the common ratio ($r \neq 1$)
- **Sum of an infinite geometric series:** The general formula for the sum S of an infinite geometric series $a_1 + a_2 + a_3 \dots$ with common ratio r where $|r| < 1$, is $S = \frac{a_1}{1 - r}$
- If an infinite geometric series has a sum, i.e. if $|r| < 1$, then the series is called a **convergent** geometric series. All other geometric (and arithmetic) series are **divergent**.
- **Synthetic Division:** Synthetic division is a shortcut method for dividing a polynomial by a linear factor of the form $(x - a)$. It can be used in place of the standard long division algorithm.
- **Zero:** If $f(x)$ is a polynomial function, then the values of x for which $f(x) = 0$ are called the **zeros** of the function. Graphically, these are the x intercepts.