

1. Convert the following angle to radians in exact form (*use π in your answer*).

$$320^\circ =$$

2. Convert the following angle to degrees.

$$\frac{7\pi}{8} \text{ radians} =$$

3. List the quadrant each angle is in.

$$\frac{17\pi}{3}$$

$$-842^\circ =$$

Write an equation of the specified function with each amplitude, period, phase shift, and vertical shift.

5. sine function: amplitude = 15, period = 4π , phase shift = $\frac{\pi}{2}$, vertical shift = -10

6. cosine function: amplitude = $\frac{2}{3}$, period = $\frac{\pi}{3}$, phase shift = $-\frac{\pi}{3}$, vertical shift = 5

7. sine function: amplitude = 6, period = π , phase shift = 0, vertical shift = $-\frac{3}{2}$

Write an equation for the tangent function where:

period: $\frac{\pi}{3}$ phase shift: $\frac{\pi}{2}$ vertical shift of -4

Write an equation for the cosecant function where:

period: π phase shift: 2π

6. cosine function: amplitude = $\frac{2}{3}$, period = $\frac{\pi}{3}$, phase shift = $-\frac{\pi}{3}$, vertical shift = 5

| | Amplitude | Trig Function | Omega, ω | X or Θ | Φ | Vertical Shift |
|----|-------------------------|-------------------|----------------------------|---------------|-------------------------------|----------------|
| Y= | | | | | | |
| | (Distance from Midline) | sin or <u>cos</u> | $\omega = \frac{2\pi}{Pd}$ | (VARIABLE) | $\Phi = -(\text{PS})(\omega)$ | (MIDLINE) |

6. cosine function: amplitude = $\frac{2}{3}$, period = $\frac{\pi}{3}$, phase shift = $-\frac{\pi}{3}$, vertical shift = 5

| | Amplitude | Trig Function | Omega, ω | X or θ | Φ | Vertical Shift |
|-----|-------------------------|---------------|----------------------------|---------------|-------------------------------|----------------|
| y = | $\frac{2}{3}$ | cos | 6 | θ | $+2\pi$ | $+5$ |
| | (Distance from Midline) | sin or cos | $\omega = \frac{2\pi}{Pd}$ | VARIABLE | $\Phi = -(\text{PS})(\omega)$ | (MIDLINE) |

$$\omega = \frac{2\pi}{\pi/3}$$
 copy change flip

$$2\pi \cdot \frac{3}{\pi} = \frac{6\pi}{\pi} = 6$$

$$\Phi = -\left(-\frac{\pi}{3}\right)(6)$$

$$\frac{\pi}{3} \cdot 6 = \frac{6\pi}{3} = 2\pi$$

$$y = \frac{2}{3}\cos(6\theta + 2\pi) + 5$$

6. cosine function: amplitude = $\frac{2}{3}$, period = $\frac{\pi}{3}$, phase shift = $-\frac{\pi}{3}$, vertical shift = 5

| | Amplitude | Trig Function | Omega, ω | X or θ | Φ | Vertical Shift |
|----|-------------------------|-------------------|----------------------------|---------------|------------------------|----------------|
| Y= | $\frac{2}{3}$ | cos | 6 | θ | $+2\pi$ | + 5 |
| | (Distance from Midline) | sin or <u>cos</u> | $\omega = \frac{2\pi}{Pd}$ | (VARIABLE) | $\Phi = -(PS)(\omega)$ | (MIDLINE) |

$$\omega = \frac{2\pi}{\frac{\pi}{3}}$$

$$2\pi \cdot \frac{3}{\pi} = \frac{6\pi}{\pi} = 6$$

$$y = \frac{2}{3} \cos(6\theta + 2\pi) + 5$$

$$\Phi = -\left(-\frac{\pi}{3}\right)(6)$$

$$= \frac{\pi}{3} \cdot \frac{6}{1} = \frac{6\pi}{3} = 2\pi$$

5. sine function: amplitude = 15, period = 4π , phase shift = $\frac{\pi}{2}$, vertical shift = -10

| | Amplitude | Trig Function | Omega, ω | X or Θ | Φ | Vertical Shift |
|----|-------------------------|-----------------------|----------------------------|---------------|------------------------|----------------|
| Y= | | | | | | |
| | (Distance from Midline) | sin or cos | $\omega = \frac{2\pi}{Pd}$ | (VARIABLE) | $\Phi = -(PS)(\omega)$ | (MIDLINE) |

5. sine function: amplitude = 15, period = 4π , phase shift = $\frac{\pi}{2}$, vertical shift = -10

| | Amplitude | Trig Function | Omega, ω | X or θ | Φ | Vertical Shift |
|----|-------------------------|-------------------|----------------------------|---------------|------------------------|----------------|
| Y= | 15 | sin | $\frac{1}{2}$ | θ | $-\frac{\pi}{4}$ | -10 |
| | (Distance from Midline) | sin or <u>cos</u> | $\omega = \frac{2\pi}{Pd}$ | (VARIABLE) | $\Phi = -(PS)(\omega)$ | (MIDLINE) |

$$\omega = \frac{2\pi}{4\pi} = \frac{1}{2}$$

$$\Phi = -\left(\frac{\pi}{2}\right)\left(\frac{1}{2}\right) = -\frac{\pi}{2} \cdot \frac{1}{2} = -\frac{\pi}{4}$$

$$y = 15 \sin\left(\frac{1}{2}\theta - \frac{\pi}{4}\right) - 10$$

5. sine function: amplitude = 15, period = 4π , phase shift = $-\frac{\pi}{2}$, vertical shift = -10

| | Amplitude | Trig Function | Omega, ω | X or θ | Φ | Vertical Shift |
|-----|-------------------------|---------------|----------------------------|---------------|-------------------------------|----------------|
| y = | 15 | sin | $\frac{1}{2}$ | θ | $-\frac{\pi}{2}$ | -10 |
| | (Distance from Midline) | sin or cos | $\omega = \frac{2\pi}{Pd}$ | (VARIABLE) | $\Phi = -(\text{PS})(\omega)$ | (MIDLINE) |

$$\omega = \frac{2\pi}{Pd}$$

$$\omega = \frac{2\pi}{4\pi}$$

$$\Phi = -\left(\frac{\pi}{2}\right)\left(\frac{1}{2}\right)$$

$$= -\frac{\pi}{2} \cdot \frac{1}{2}$$

$$= -\frac{\pi}{4}$$

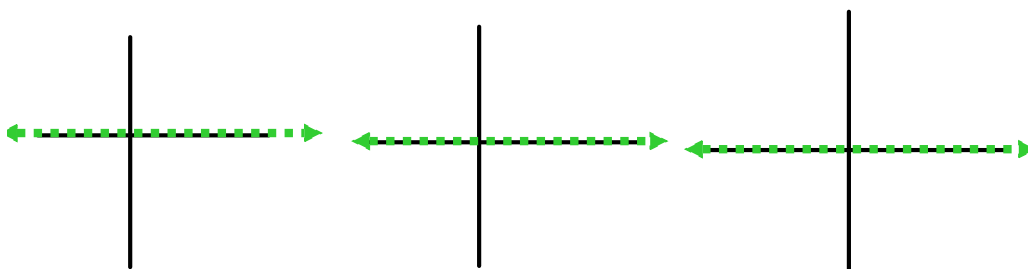
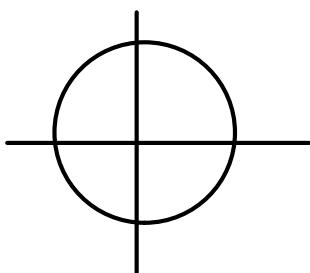
$$y = 15 \sin\left(\frac{1}{2}\theta - \frac{\pi}{4}\right) - 10 = \frac{2\pi}{4} \cdot \frac{1}{2}$$

Ex. 1

Kiki and Mikey are riding on a ferris wheel at a local carnival. The circular ferris wheel has a radius of 50 feet and is located 60 feet from the ground level. The ferris wheel makes a full rotation every 20 minutes. As a function relating the height of Kiki and Mikey on the ferris wheel to the time they ride (in minutes), find the following:

- a) the amplitude of the seat.
- b) the period of the seat.
- c) the equilibrium of the ride.
- d) an equation modeling the data presented.

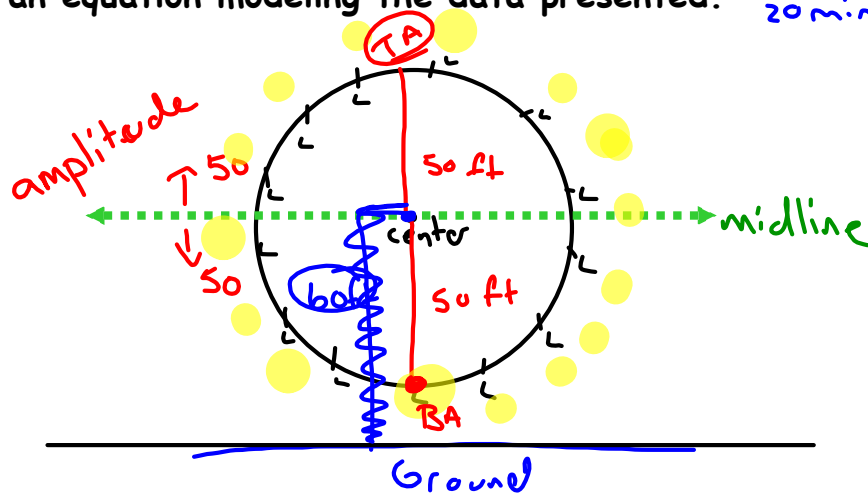
| | Amplitude | Trig Function | Omega, ω | X or Θ | Φ | Vertical Shift |
|----|-------------------------|-------------------|----------------------------|---------------|------------------------|----------------|
| Y= | | | | | | |
| | (Distance from Midline) | sin or <u>cos</u> | $\omega = \frac{2\pi}{Pd}$ | (VARIABLE) | $\Phi = -(PS)(\omega)$ | (MIDLINE) |

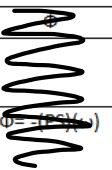
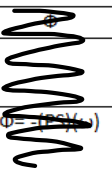


Ex. 1

Kiki and Mikey are riding on a ferris wheel at a local carnival. The circular ferris wheel has a radius of 50 feet and is located 60 feet from the ground level. The ferris wheel makes a full rotation every 20 minutes. As a function relating the height of Kiki and Mikey on the ferris wheel to the time they ride (in minutes), find the following:

- a) the amplitude of the seat. 50
- b) the period of the seat. 20 min
- c) the equilibrium of the ride.
- d) an equation modeling the data presented. 20 min.

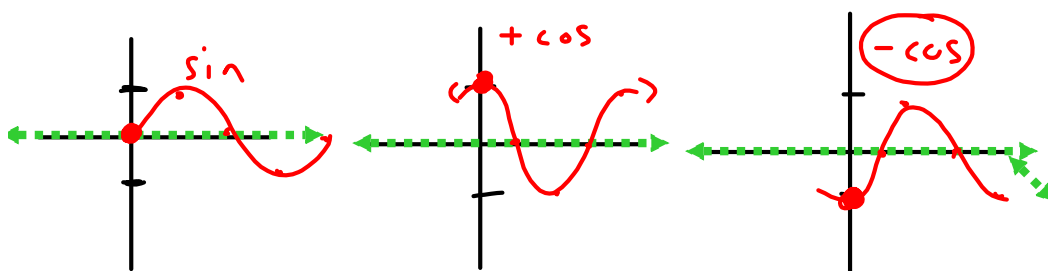


| | Amplitude | Trig Function | Omega, ω | X or θ |  | Vertical Shift |
|----|-------------------------|---------------|----------------------------|---------------|---|----------------|
| Y= | 50 | -cos | $\frac{\pi}{10}$ | θ |  | 60 |
| | (Distance from Midline) | sin or cos | $\omega = \frac{2\pi}{Pd}$ | (VARIABLE) | $\theta = t \cdot \omega$ | (MIDLINE) |

$pd = 20 \text{ min}$

$\omega = \frac{2\pi}{20} = \frac{\pi}{10}$

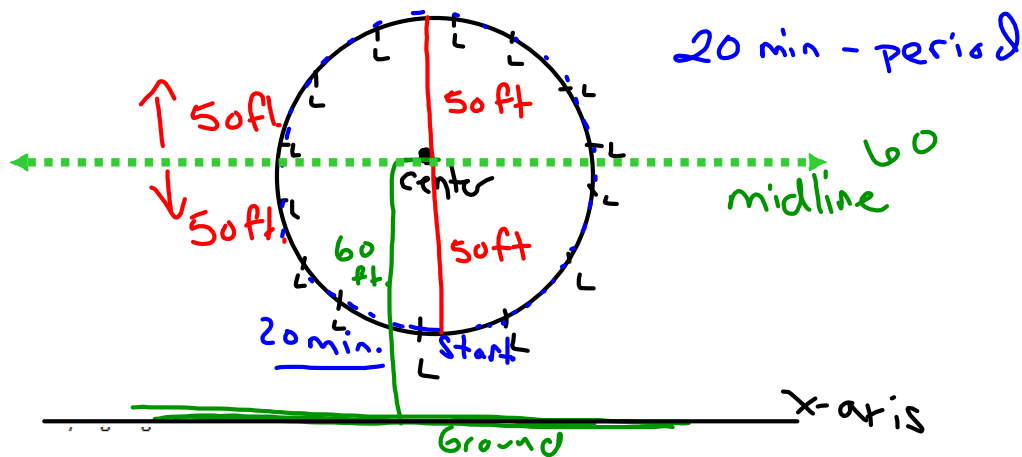
$y = -50 \cos\left(\frac{\pi}{10} \theta\right)$



Ex. 1

Kiki and Mikey are riding on a ferris wheel at a local carnival. The circular ferris wheel has a radius of 50 feet and is located 60 feet from the ground level. The ferris wheel makes a full rotation every 20 minutes. As a function relating the height of Kiki and Mikey on the ferris wheel to the time they ride (in minutes), find the following:

- a) the amplitude of the seat. **50 ft.**
- b) the period of the seat **20 min.**
- c) the equilibrium of the ride. **midline 60 ft.**
- d) an equation modeling the data presented.



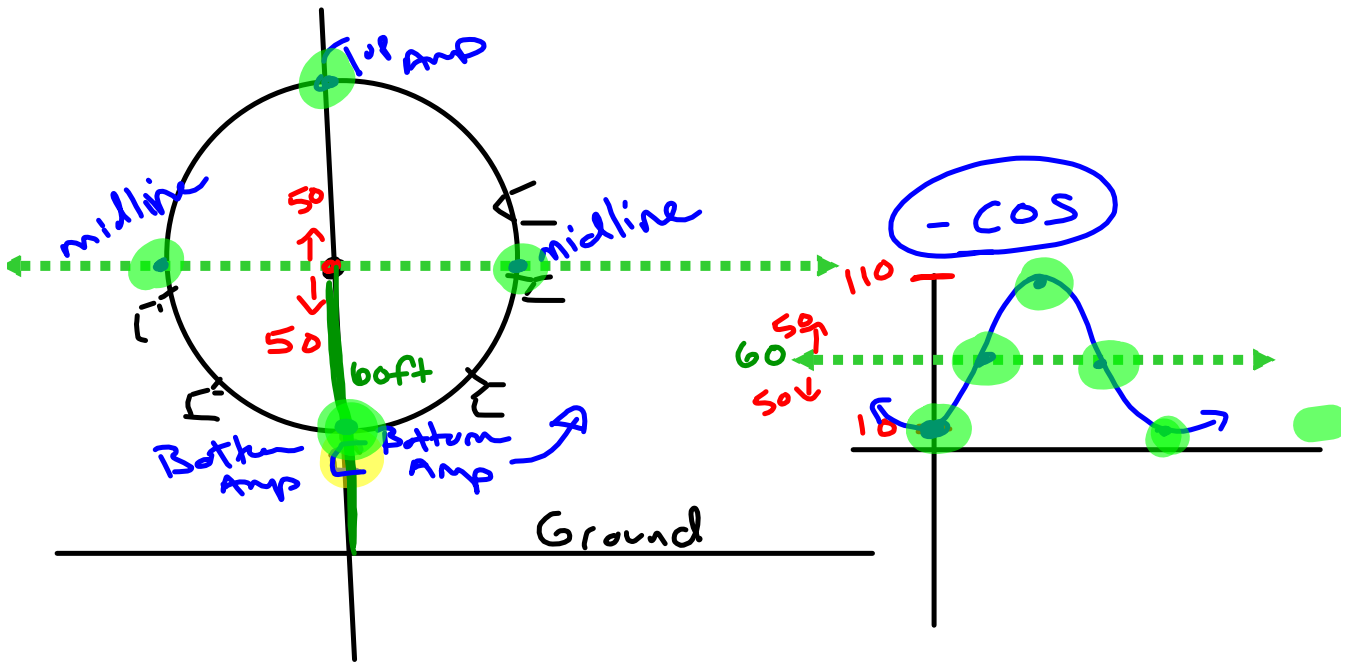
| | Amplitude | Trig Function | Omega, ω | X or θ | | Vertical Shift |
|-------|-------------------------|---------------------------|------------------------------------|----------------------------|--|----------------|
| $y =$ | 50 | $-\cos$ | $\frac{\pi}{10}$ | θ | | 60 |
| | (Distance from Midline) | sin or <u>cos</u> | $\omega = \frac{2\pi}{Pd}$ | (VARIABLE) | | (MIDLINE) |

$\omega = \frac{2\pi}{Pd} = \frac{2\pi}{20 \text{ min.}}$

$\omega = \frac{2\pi}{20}$

$= \frac{\pi}{10}$

$y = -50 \cos\left(\frac{\pi}{10} \theta\right) + 60$



Example 2:

An evil litterer tosses a half-full (or half-empty) bottle of water into the sea. As the water moves the bottle bobs up and down. The distance between its highest and lowest point is 5 cm. It moves from the highest to the lowest point in 3 seconds and then back to the highest point 3 seconds later and so on.

Write a cos function that models the movement of the littered bottle in relationship to the equilibrium point.



| | Amplitude | Trig Function | Omega, ω | X or θ | Φ | Vertical Shift |
|----|-------------------------|-------------------|----------------------------|---------------|------------------------|----------------|
| Y= | | | | | | |
| | (Distance from Midline) | sin or <u>cos</u> | $\omega = \frac{2\pi}{Pd}$ | (VARIABLE) | $\Phi = -(PS)(\omega)$ | (MIDLINE) |

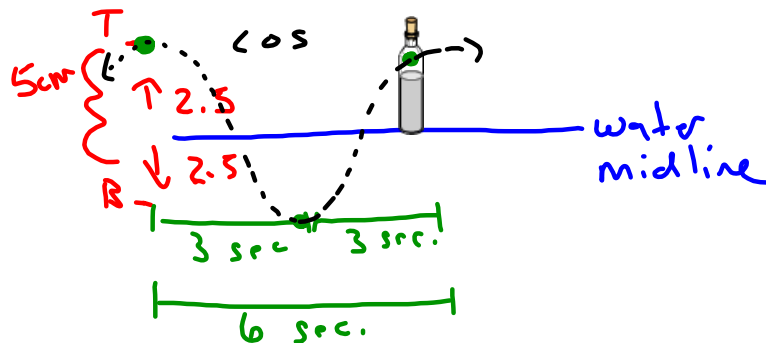
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Write a cos function that models the movement of the littered bottle in relationship to the equilibrium point.

Amp: 2.5

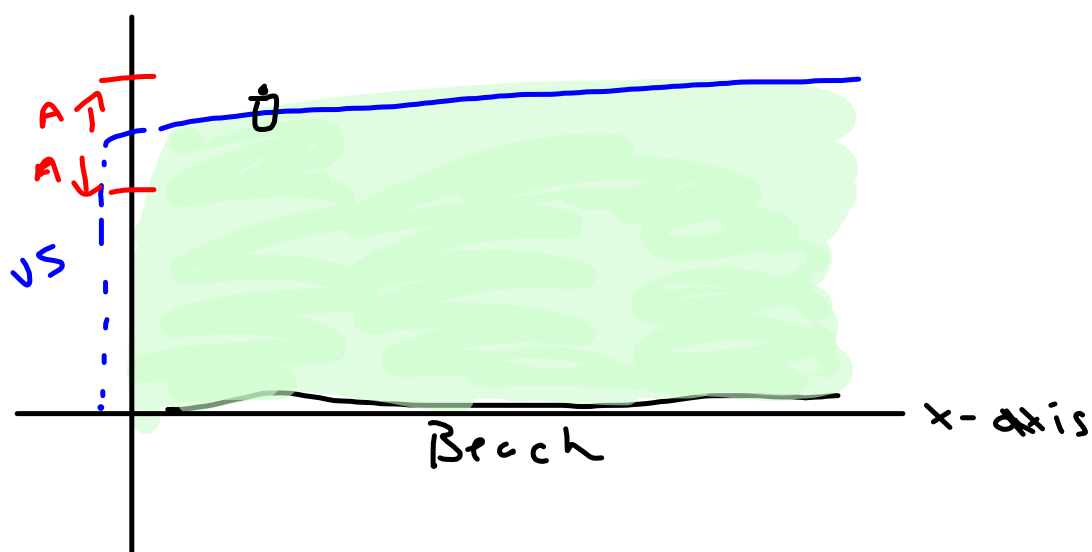
period: 6



| | Amplitude | Trig Function | Omega, ω | X or θ | ϕ | Vertical Shift |
|-------|-------------------------|-----------------------|---|---------------|--|----------------|
| $y =$ | <u>2.5</u> | <u>cos</u> | $\frac{\pi}{3}$ | θ | W | W |
| | (Distance from Midline) | sin or cos | $\omega = \frac{2\pi}{Pd} = \frac{2\pi}{6}$ | (VARIABLE) | $\phi = -(\text{PSI})$ | (MIDLINE) |

$\omega = \frac{2\pi}{6}$
 $\omega = \frac{\pi}{3}$

$y = 2.5 \cos\left(\frac{\pi}{3} \theta\right)$



Example 3: HW: p. 391 (7-12)

Write a sine function which models the oscillation of tides in KEY WEST, Florida if the equilibrium point is 7.8 feet, the amplitude is 5.5 feet, the phase shift is -2.0 hours, and the period is 12.4 hours. According to your model, find the average position of the tides after 7 hours.